

## 1.6 Solving Eqns W/Variables on Both Sides

### Solving Equations with Variables on Both Sides

- ① • Eliminate grouping symbols by using the distributive property or eliminate fractions by multiplying all terms by the LCD or a common multiple.
- ③ • Move the variable to one side of the equation by adding or subtracting.
- ④ • Move the constant to the Other Side of the equation by adding or subtracting.
- ② • Combine like terms if there is any on either side of equal sign
- ⑤ • Isolate the variable by multiplying or dividing the variable's coefficient  
 • It does not MATTER which side the variable is on. Pick a side and keep it consistent. \* Variables on the LEFT SIDE, make life easier in Unit 2! \*

Example 1: Solve each equation. USE A SEPARATE SHEET TO DO EXAMPLES ON.

a.)  $5y + 2 = 2y - 4$

$\{ \begin{matrix} 5y \\ -2 \end{matrix} \}$

b.)  $2n - 5 = 8n + 1$

$\{ \begin{matrix} 2n \\ -13 \end{matrix} \}$

c.)  $4x + 6 - 11 = x - 8x - 5$

$\{ \begin{matrix} 4x \\ 0 \end{matrix} \}$

d.)  $2(x+1) - 5 = 3 - (6x+2)$

$\{ \begin{matrix} y \\ 2 \end{matrix} \}$

e.)  $\frac{5}{6}x - \frac{1}{3} = \frac{3}{4}x + 2$

$\{ \begin{matrix} x \\ 28 \end{matrix} \}$

f.)  $0.08x - 3 = 0.4x + 1$

$\{ \begin{matrix} x \\ -12.5 \end{matrix} \}$

g.)  $\frac{x}{5} = \frac{6}{4}$

$\{ \begin{matrix} x \\ 7.5 \end{matrix} \}$

h.)  $\frac{b+2}{14} = \frac{b}{10}$

$\{ \begin{matrix} b \\ 5 \end{matrix} \}$

i.)  $\frac{w+3}{4} = \frac{w-4}{6}$

$\{ \begin{matrix} w \\ -17 \end{matrix} \}$

\_\_\_\_\_ (aka opposite angles) are \_\_\_\_\_ of each other when two lines \_\_\_\_\_. These angles are \_\_\_\_\_ (or equal) to each other.



Example 1:*Move variables!*

a)  $5y + 2 = 2y - 4$

$\underline{-2y} \quad \underline{-2y}$

$3y + 2 = -4$   
 $\underline{-2} \quad \underline{-2}$

$\frac{3y}{3} = -6$

$y = -2$

{-2}

b)  $2n - 5 = 8n + 1$

$\underline{-3n} \quad \underline{-3n}$

$-6n - 5 = 1$   
 $\underline{+5} \quad \underline{+5}$

$\frac{-6n}{-6} = \frac{6}{-6}$

$n = -1$

{-1}

c)  $4x + 6 - 11 = x - 8x - 5$  combine  
 $4x \cancel{+ 6 - 11} = \cancel{x - 8x} - 5$  *Like Terms!*

$4x - 5 = -7x - 5$

$\underline{+7x} \quad \underline{+7x}$

$11x - 5 = -5$   
 $\underline{+5} \quad \underline{+5}$

$\frac{11x}{11} = \frac{0}{11}$

$x = 0$

{0}

d)  $2(x+1) - 5 = 3 - 1(6x+2)$   
*distribute first!*

$2x \cancel{+ 2} - 5 = 3 - 6x \cancel{+ 2}$

$2x - 3 = 1 - 6x$   
 $\underline{+6x} \quad \underline{+6x}$

*combine like terms!*

$8x - 3 = 1$   
 $\underline{+3} \quad \underline{+3}$

$\frac{8x}{8} = \frac{4}{8}$

$x = \frac{4}{8}$  *Reduce*

$x = .5 \text{ or } 1/2$

{1/2}

Denominators: 6, 3, 4, 1

c)  $\frac{5}{6}x - \frac{1}{3} = \frac{3}{4}x + 2$  LCD 12 or common multiple 72  
 $6 \cdot 3 \cdot 4 \cdot 1 \rightarrow$

$12\left(\frac{5}{6}x - \frac{1}{3}\right) = 12\left(\frac{3}{4}x + 2\right)$

$10x - 4 = 9x + 24$  NO MORE FRACTIONS!  
 $\cancel{-9x}$   $\cancel{-9x}$  YEA!! ☺

$x - 4 = 24$   
 $\cancel{+4}$   $\cancel{+4}$

$x = 28$

{28}

f)  $0.08x - 3 = 0.4x + 1$   
 $\cancel{-0.4x}$   $\cancel{-0.4x}$

$-0.32x - 3 = 1$   
 $\cancel{+3}$   $\cancel{+3}$

$\frac{-0.32x}{-0.32} = \frac{4}{-0.32}$

$x = -12.5$

{-12.5}

g)  ~~$\frac{x}{5} = \frac{6}{4}$~~  cross multiply

$\frac{4x}{4} = \frac{30}{4}$

$x = \frac{30}{4}$  REDUCE

$x = \frac{15}{2}$  or 7.5

{7.5}

h)  $\frac{b+2}{14} = \frac{b}{10}$

~~$\frac{b+2}{14} = \frac{b}{10}$~~

$14b = 10(b+2)$

$14b = 10b + 20$   
 $\cancel{10b}$   $\cancel{10b}$

$\frac{4b}{4} = \frac{20}{4}$   $b = 5$

i)  $\frac{w+3}{4} = \frac{w-4}{6}$

~~$\frac{w+3}{4} = \frac{w-4}{6}$~~

$6(w+3) = 4(w-4)$

$6w + 18 = 4w - 16$   
 $\cancel{4w}$   $\cancel{4w}$

$2w + 18 = -16$

$\cancel{-18}$   $\cancel{-18}$   
 $2w = -34$

$\frac{2w}{2} = \frac{-34}{2}$

$w = -17$

{-17}