

Writing Domain/Range – Inequality Notation Vs. Interval Notation

Inequality notation → rewriting expressions using the six inequality symbols which are ...

Interval notation → rewriting inequalities using numbers, infinity symbols $-\infty$ or ∞

* Small #, large # and/or both with grouping symbols such as brackets $[]$ and parentheses $()$

• brackets represent: CLOSE DOTS and UNDERLINED Inequalities such as \leq , \geq , or $=$

• parentheses represents Open DOTS and NOT-underlined inequalities such as $<$, $>$, or \neq

• If you have more than 1 interval (or “area of shading”), then you must use union symbol \cup

Example 1: Complete the chart below using the appropriate notation(s). * Infinity symbols always get ()

	Inequality Notation	Interval Notation	Graph (on a number line)
a.)	$x > 2$	$(2, \infty)$	
b.)	$x \leq -1$	$(-\infty, -1]$	
c.)	Compound "AND" $-4 < x \leq 0$	$(-4, 0]$	
d.)	<u>all real numbers</u> (IR) symbol	$(-\infty, \infty)$	
e.)	* All real numbers IR, $x \neq -3$	$(-\infty, -3) \cup (-3, \infty)$	
f.)	Compound "OR" $x < -2$ or $x \geq 1$	$(-\infty, -2) \cup [1, \infty)$	

– **domain (of a graph)** → set of all x-values in which a function is defined (look Left → Right only look at x-values)

– **range (of a graph)** → set of all y-values in which a function is defined (look Bottom → Top only look at y-values.)

Example 2: Determine the domain and range (using both notations) of each given graph.

Example 2a	Example 2b	Example 2c	Example 2d
D/R – Using an Inequality D: $x = \mathbb{R}$ * All real numbers R: $y \geq -4$	D/R – Using an Inequality D: $x > -4$ R: $y > -2$	D/R – Using an Inequality D: $x = \mathbb{R}, \neq -2$ R: $y < 3$	D/R – Using an Inequality D: $-4 \leq x < 2$ R: $-3 < y \leq 3$
D/R – Using an Interval D: $(-\infty, \infty)$ R: $[-4, \infty)$	D/R – Using an Interval D: $(-4, \infty)$ R: $(-2, \infty)$	D/R – Using an Interval D: $(-\infty, -2) \cup (-2, \infty)$ R: $(-\infty, 3)$	D/R – Using an Interval D: $[-4, 2)$ R: $(-3, 3]$

Graphing Quadratic Functions Using Transformations (slides, reflections, vertical compression/stretch)

Characteristics of Parent Quadratic Function

Parent Function of a Quadratic: $y = x^2$

x	y
-1	1
0	0
1	1

- Vertex Pt: $(0,0)$
- Domain: $(-\infty, \infty)$
- AOS: $x=0$
- Range: $[0, \infty)$

** X-coord. of the vertex is the AOS.*

Transformation # 1 – Vertical Translations

If have $y = x^2 \pm d$ then you can have ... *Not in ()!*

- $+d$ which means translates UP " d " units
- $-d$ which means translates DOWN " d " units

You will add or subtract from y-coord

Transformation # 2 – Horizontal Translations

If have $y = (x \pm c)^2$ then you can have ...

- $+c$ which means translates LEFT " c " units
- $-c$ which means translates RIGHT " c " units

You will add or subtract from x-coord

Transformation # 3 – Reflection

If have $y = -x^2$ then you have...

a Reflection about x-axis causing function to flip down.

Example 3: Do the following –

- Draw in the original quadratic parent graph. *reflection, DO the reflection first*
- State all the transformations in the given function.
- Graph the given function based on its transformations.
- State the domain and range of graphed/transformed function only using interval notation.

Example 3a

Given Function: $y = (x+2)^2 - 3$

Transformations: left 2 units, down 3 units!

Domain (of given funct): $(-\infty, \infty)$

Range (of given funct): $[-3, \infty)$

Example 3b

Given Function: $y = (x-3)^2 + 1$

Transformations: Right 3, up 1

Domain (of given funct): $(-\infty, \infty)$

Range (of given funct): $[1, \infty)$

Example 3c

Given Function: $y = -(x+4)^2 + 2$

Transformations: Reflect x-axis, left 4, up 2

** Do the reflect first!*

Domain (of given funct): $(-\infty, \infty)$

Range (of given funct): $(-\infty, 2]$